

Needs["General`Lorentz`"]

General`Lorentz` loaded. Click for symbols.

In[3]:= ?General`Lorentz`*

General`Lorentz`

[Absorption](#) [Dispersion](#) [Lorentz](#)

Absorption[w, {amp, w0, lam}] generates a Absorption Lorentzian function of w with amplitude amp, centre freq w0, and hwhh = lam;

Absorption[w, {w0, lam}] assumes unit amplitude;

Absorption[w, {{_, _, _}...}] generates a superposition of such Absorption Lorentzians

In[6]:= ?? Absorption

In[16]:= (Im[*] ^= 0) & /@ {w, Rea, Ima, w0, lam, k}

UpSet::write : Tag Re in Im[Re[a]] is Protected. [More...](#)

UpSet::write : Tag Im in Im[Im[a]] is Protected. [More...](#)

Out[16]= {0, 0, 0, 0, 0, 0}

In[12]:= Absorption[w, {Rea, w0, lam}]

Out[12]=
$$\frac{\text{lam Rea}}{\text{lam}^2 + (w - w0)^2}$$

In[13]:= Dispersion[w, {Ima, w0, lam}]

Out[13]=
$$\frac{\text{Ima} (w - w0)}{\text{lam}^2 + (w - w0)^2}$$

In[14]:= ReLor[w_, {a_, w0_, lam_}] = (Rea = Re[a]; Ima = Im[a]; Absorption[w, {Rea, w0, lam}]) + Dispersion[w, {Ima, w0, lam}]

Out[14]=
$$\frac{(w - w0) \text{Im}[a]}{\text{lam}^2 + (w - w0)^2} + \frac{\text{lam Re}[a]}{\text{lam}^2 + (w - w0)^2}$$

In[18]:= Sqrt[-(k^2 - (WD/2)^2)]; ReLor[W, {(1 - I*k/R)/2, R, k}] + ReLor[W, {(1 + I*k/R)/2, -R, k}]

Out[19]=
$$\frac{k \left(\frac{1}{2} - \frac{1}{2} k \text{Im} \left[\frac{1}{\sqrt{-k^2 + \frac{WD^2}{4}}} \right] \right)}{k^2 + \left(W + \sqrt{-k^2 + \frac{WD^2}{4}} \right)^2} + \frac{k \left(\frac{1}{2} + \frac{1}{2} k \text{Im} \left[\frac{1}{\sqrt{-k^2 + \frac{WD^2}{4}}} \right] \right)}{k^2 + \left(W - \sqrt{-k^2 + \frac{WD^2}{4}} \right)^2} - \frac{k \left(W - \sqrt{-k^2 + \frac{WD^2}{4}} \right) \text{Re} \left[\frac{1}{\sqrt{-k^2 + \frac{WD^2}{4}}} \right]}{2 \left(k^2 + \left(W - \sqrt{-k^2 + \frac{WD^2}{4}} \right)^2 \right)} + \frac{k \left(W + \sqrt{-k^2 + \frac{WD^2}{4}} \right) \text{Re} \left[\frac{1}{\sqrt{-k^2 + \frac{WD^2}{4}}} \right]}{2 \left(k^2 + \left(W + \sqrt{-k^2 + \frac{WD^2}{4}} \right)^2 \right)}$$

In[20]:= * /. {Im[_] -> 0, Re[arg_] -> arg}

General::spell1 : Possible spelling error: new symbol name "arg" is similar to existing symbol "Arg". [More...](#)

Out[20]=
$$\frac{k}{2 \left(k^2 + \left(W - \sqrt{-k^2 + \frac{WD^2}{4}} \right)^2 \right)} - \frac{k \left(W - \sqrt{-k^2 + \frac{WD^2}{4}} \right)}{2 \sqrt{-k^2 + \frac{WD^2}{4}} \left(k^2 + \left(W - \sqrt{-k^2 + \frac{WD^2}{4}} \right)^2 \right)} + \frac{k}{2 \left(k^2 + \left(W + \sqrt{-k^2 + \frac{WD^2}{4}} \right)^2 \right)} + \frac{k \left(W + \sqrt{-k^2 + \frac{WD^2}{4}} \right)}{2 \sqrt{-k^2 + \frac{WD^2}{4}} \left(k^2 + \left(W + \sqrt{-k^2 + \frac{WD^2}{4}} \right)^2 \right)}$$

In[21]:= * // ExpandAll

Out[21]=
$$\frac{k}{2 W^2 + \frac{WD^2}{2} - 4 W \sqrt{-k^2 + \frac{WD^2}{4}}} + \frac{k}{2 W^2 + \frac{WD^2}{2} + 4 W \sqrt{-k^2 + \frac{WD^2}{4}}} - \frac{k W}{4 k^2 W - W WD^2 + 2 W^2 \sqrt{-k^2 + \frac{WD^2}{4}} + \frac{1}{2} WD^2 \sqrt{-k^2 + \frac{WD^2}{4}}} + \frac{k \sqrt{-k^2 + \frac{WD^2}{4}}}{4 k^2 W - W WD^2 + 2 W^2 \sqrt{-k^2 + \frac{WD^2}{4}} + \frac{1}{2} WD^2 \sqrt{-k^2 + \frac{WD^2}{4}}} + \frac{k W}{-4 k^2 W + W WD^2 + 2 W^2 \sqrt{-k^2 + \frac{WD^2}{4}} + \frac{1}{2} WD^2 \sqrt{-k^2 + \frac{WD^2}{4}}} + \frac{k \sqrt{-k^2 + \frac{WD^2}{4}}}{-4 k^2 W + W WD^2 + 2 W^2 \sqrt{-k^2 + \frac{WD^2}{4}} + \frac{1}{2} WD^2 \sqrt{-k^2 + \frac{WD^2}{4}}}$$

In[22]:= * // Together

Out[22]=
$$\frac{(8 (256 k^5 W^2 WD^2 + 64 k^3 W^4 WD^2 - 96 k^3 W^2 WD^4 - 16 k W^4 WD^4 + 4 k^3 WD^6 + 8 k W^2 WD^6 - k WD^8))}{\left((-4 W^2 - WD^2 + 4 W \sqrt{-4 k^2 + WD^2}) (4 W^2 + WD^2 + 4 W \sqrt{-4 k^2 + WD^2}) (16 k^2 W - 4 W WD^2 + 4 W^2 \sqrt{-4 k^2 + WD^2} + WD^2 \sqrt{-4 k^2 + WD^2}) (-16 k^2 W + 4 W WD^2 + 4 W^2 \sqrt{-4 k^2 + WD^2} + WD^2 \sqrt{-4 k^2 + WD^2}) \right)}$$

In[23]:= * // ExpandAll

Out[23]=
$$\frac{(2048 k^5 W^2 WD^2)}{(16384 k^6 W^4 + 8192 k^4 W^6 + 1024 k^2 W^8 - 8192 k^4 W^4 WD^2 - 3072 k^2 W^6 WD^2 - 256 W^8 WD^2 + 512 k^4 W^2 WD^4 + 1408 k^2 W^4 WD^4 + 256 W^6 WD^4 - 192 k^2 W^2 WD^6 - 96 W^4 WD^6 + 4 k^2 WD^8 + 16 W^2 WD^8 - WD^{10}) + (512 k^3 W^4 WD^2) / (16384 k^6 W^4 + 8192 k^4 W^6 + 1024 k^2 W^8 - 8192 k^4 W^4 WD^2 - 3072 k^2 W^6 WD^2 - 256 W^8 WD^2 + 512 k^4 W^2 WD^4 + 1408 k^2 W^4 WD^4 + 256 W^6 WD^4 - 192 k^2 W^2 WD^6 - 96 W^4 WD^6 + 4 k^2 WD^8 + 16 W^2 WD^8 - WD^{10}) - (768 k^3 W^2 WD^4) / (16384 k^6 W^4 + 8192 k^4 W^6 + 1024 k^2 W^8 - 8192 k^4 W^4 WD^2 - 3072 k^2 W^6 WD^2 - 256 W^8 WD^2 + 512 k^4 W^2 WD^4 + 1408 k^2 W^4 WD^4 + 256 W^6 WD^4 - 192 k^2 W^2 WD^6 - 96 W^4 WD^6 + 4 k^2 WD^8 + 16 W^2 WD^8 - WD^{10}) - (128 k W^4 WD^4) / (16384 k^6 W^4 + 8192 k^4 W^6 + 1024 k^2 W^8 - 8192 k^4 W^4 WD^2 - 3072 k^2 W^6 WD^2 - 256 W^8 WD^2 + 512 k^4 W^2 WD^4 + 1408 k^2 W^4 WD^4 + 256 W^6 WD^4 - 192 k^2 W^2 WD^6 - 96 W^4 WD^6 + 4 k^2 WD^8 + 16 W^2 WD^8 - WD^{10}) + (32 k^3 WD^6) / (16384 k^6 W^4 + 8192 k^4 W^6 + 1024 k^2 W^8 - 8192 k^4 W^4 WD^2 - 3072 k^2 W^6 WD^2 - 256 W^8 WD^2 + 512 k^4 W^2 WD^4 + 1408 k^2 W^4 WD^4 + 256 W^6 WD^4 - 192 k^2 W^2 WD^6 - 96 W^4 WD^6 + 4 k^2 WD^8 + 16 W^2 WD^8 - WD^{10}) + (64 k W^2 WD^6) / (16384 k^6 W^4 + 8192 k^4 W^6 + 1024 k^2 W^8 - 8192 k^4 W^4 WD^2 - 3072 k^2 W^6 WD^2 - 256 W^8 WD^2 + 512 k^4 W^2 WD^4 + 1408 k^2 W^4 WD^4 + 256 W^6 WD^4 - 192 k^2 W^2 WD^6 - 96 W^4 WD^6 + 4 k^2 WD^8 + 16 W^2 WD^8 - WD^{10}) - (8 k WD^8) / (16384 k^6 W^4 + 8192 k^4 W^6 + 1024 k^2 W^8 - 8192 k^4 W^4 WD^2 - 3072 k^2 W^6 WD^2 - 256 W^8 WD^2 + 512 k^4 W^2 WD^4 + 1408 k^2 W^4 WD^4 + 256 W^6 WD^4 - 192 k^2 W^2 WD^6 - 96 W^4 WD^6 + 4 k^2 WD^8 + 16 W^2 WD^8 - WD^{10})}$$

In[24]:= * // Together

Out[24]=
$$\frac{8 k WD^2}{64 k^2 W^2 + 16 W^4 - 8 W^2 WD^2 + WD^4}$$

In[25]:= * // Simplify

Out[25]=
$$\frac{8 k WD^2}{64 k^2 W^2 + (-4 W^2 + WD^2)^2}$$